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Advanced Series in Mathematical Physics
Vol. 17

BRAID GROUP, KNOT THEORY AND STATISTICAL MECHANICS II

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World Scientific

Singapore • New Jersey • London • Hong Kong

Published by

World Scientific Publishing Co. Pte. Ltd.

P O Box 128, Farrer Road, Singapore 9128

USA office: Suite 1B, 1060 Main Street, River Edge, NJ 07661

UK office: 73 Lynton Mead, Totteridge, London N20 8DH

**BRAID GROUP, KNOT THEORY AND
STATISTICAL MECHANICS, II**

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ISBN 981-02-1524-X

Printed in Singapore by Utopia Press.

FOREWORD

It has been four years since the publication in 1989 of the previous volume bearing the same title as the present one. An enormous amount of work has been done in the meantime. We hope the present volume will provide a summary of some of these works which are still progressing in several directions.

Chen Ning Yang
Mo-Lin Ge

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